

$$\begin{aligned}
 & \text{1.} & \text{2.} & \text{3.} \\
 \cos. p &= \frac{\sin. a \sin. \frac{1}{2} B \sin. \frac{1}{2} C}{\cos. \frac{1}{2} A} = \frac{\sin. b \sin. \frac{1}{2} A \sin. \frac{1}{2} C}{\cos. \frac{1}{2} B} = \frac{\sin. c \sin. \frac{1}{2} A \sin. \frac{1}{2} B}{\cos. \frac{1}{2} C}; \\
 & \text{4.} & \text{5.} & \text{6.} \\
 \cos. (p - a) &= \frac{\sin. a \cos. \frac{1}{2} B \cos. \frac{1}{2} C}{\cos. \frac{1}{2} A} = \frac{\sin. c \sin. \frac{1}{2} A \cos. \frac{1}{2} B}{\sin. \frac{1}{2} C} = \frac{\sin. b \sin. \frac{1}{2} A \cos. \frac{1}{2} C}{\sin. \frac{1}{2} B}; \\
 & \text{7.} & \text{8.} & \text{9.} \\
 \cos. (p - b) &= \frac{\sin. b \cos. \frac{1}{2} A \cos. \frac{1}{2} C}{\cos. \frac{1}{2} B} = \frac{\sin. a \sin. \frac{1}{2} B \cos. \frac{1}{2} C}{\sin. \frac{1}{2} A} = \frac{\sin. c \cos. \frac{1}{2} A \sin. \frac{1}{2} B}{\sin. \frac{1}{2} C}; \\
 & \text{10.} & \text{11.} & \text{12.} \\
 \cos. (p - c) &= \frac{\sin. c \cos. \frac{1}{2} A \cos. \frac{1}{2} B}{\cos. \frac{1}{2} C} = \frac{\sin. b \cos. \frac{1}{2} A \sin. \frac{1}{2} C}{\sin. \frac{1}{2} B} = \frac{\sin. a \cos. \frac{1}{2} B \sin. \frac{1}{2} C}{\sin. \frac{1}{2} A}.
 \end{aligned}$$

$$\begin{aligned}
 & \text{13.} & \text{14.} & \text{15.} \\
 \sin. P &= \frac{\sin. A \cos. \frac{1}{2} b \cos. \frac{1}{2} c}{\sin. \frac{1}{2} a} = \frac{\sin. B \cos. \frac{1}{2} a \cos. \frac{1}{2} c}{\sin. \frac{1}{2} b} = \frac{\sin. C \cos. \frac{1}{2} a \cos. \frac{1}{2} b}{\sin. \frac{1}{2} c}; \\
 & \text{16.} & \text{17.} & \text{18.} \\
 \sin. (P - A) &= \frac{\sin. A \sin. \frac{1}{2} b \sin. \frac{1}{2} c}{\sin. \frac{1}{2} a} = \frac{\sin. C \cos. \frac{1}{2} a \sin. \frac{1}{2} b}{\cos. \frac{1}{2} c} = \frac{\sin. B \cos. \frac{1}{2} a \sin. \frac{1}{2} c}{\cos. \frac{1}{2} b}; \\
 & \text{19.} & \text{20.} & \text{21.} \\
 \sin. (P - B) &= \frac{\sin. B \sin. \frac{1}{2} a \sin. \frac{1}{2} c}{\sin. \frac{1}{2} b} = \frac{\sin. A \cos. \frac{1}{2} b \sin. \frac{1}{2} c}{\cos. \frac{1}{2} a} = \frac{\sin. C \sin. \frac{1}{2} a \cos. \frac{1}{2} b}{\cos. \frac{1}{2} c}; \\
 & \text{22.} & \text{23.} & \text{24.} \\
 \sin. (P - C) &= \frac{\sin. C \sin. \frac{1}{2} a \sin. \frac{1}{2} b}{\sin. \frac{1}{2} c} = \frac{\sin. B \sin. \frac{1}{2} a \cos. \frac{1}{2} c}{\cos. \frac{1}{2} b} = \frac{\sin. A \sin. \frac{1}{2} b \cos. \frac{1}{2} c}{\cos. \frac{1}{2} a}.
 \end{aligned}$$

Daß sich aus je 2 neben einander stehenden die Gleichung §. 13. I. sogleich ergibt, leuchtet von selbst ein.

Durch einfache Multiplication je zweier zweckmäßig gewählter finden sich nun folgende 4 Gleichungen, welche man sonst durch Umwandlung hervorzubringen pflegt.